

AD-753 350

CHARACTERISTICS OF THE TURBULENT
DIFFUSION PARAMETERS AS RELATED
TO STABILITY

Manuel Armendariz, et al

Army Electronics Command
White Sands Missile Range, New Mexico

November 1972.

DISTRIBUTED BY:

NTIS

National Technical Information Service
U. S. DEPARTMENT OF COMMERCE
5285 Port Royal Road, Springfield Va. 22151



AD 753350

AD

Reports Control Symbol
OSD-1366

RESEARCH AND DEVELOPMENT TECHNICAL REPORT
ECOM-5468

CHARACTERISTICS OF THE TURBULENT DIFFUSION PARAMETERS AS RELATED TO STABILITY

By

Manuel Armendariz

James R. Scoggins

Texas A & M University

November 1972

Approved for public release; distribution unlimited.

ECOM

UNITED STATES ARMY ELECTRONICS COMMAND - FORT MONMOUTH, NEW JERSEY

Reproduced by
NATIONAL TECHNICAL
INFORMATION SERVICE
U S Department of Commerce
Springfield VA 22151

35

NOTICES

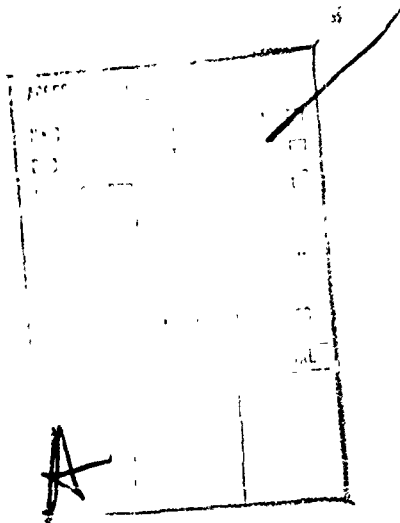
Disclaimers

The findings in this report are not to be construed as an official Department of the Army position, unless so designated by other authorized documents.

The citation of trade names and names of manufacturers in this report is not to be construed as official Government indorsement or approval of commercial products or services referenced herein.

Disposition

Destroy this report when it is no longer needed. Do not return it to the originator.



UNCLASSIFIED

Security Classification

DOCUMENT CONTROL DATA - R & D

(Security classification of title, body of abstract and indexing annotation must be entered when the overall report is classified)

1. ORIGINATING ACTIVITY (Corporate author)		2a. REPORT SECURITY CLASSIFICATION	
Atmospheric Sciences Laboratory White Sands Missile Range, New Mexico		Unclassified	
		2b. GROUP	
3. REPORT TITLE			
CHARACTERISTICS OF THE TURBULENT DIFFUSION PARAMETERS AS RELATED TO STABILITY			
4. DESCRIPTIVE NOTES (Type of report and inclusive dates)			
5. AUTHOR(S) (First name, middle initial, last name)			
Manuel Armendariz and James R. Scoggins			
6. REPORT DATE		7a. TOTAL NO. OF PAGES	7b. NO. OF REFS
November 1972		23 34	8
8a. CONTRACT OR GRANT NO.		8b. ORIGINATOR'S REPORT NUMBER(S)	
a. PROJECT NO.		ECOM-5468	
c. DA Task No. IT061102B53A-17		9b. OTHER REPORT NO(S) (Any other numbers that may be assigned this report)	
d.			
10. DISTRIBUTION STATEMENT			
Approved for public release; distribution unlimited.			
11. SUPPLEMENTARY NOTES		12. SPONSORING MILITARY ACTIVITY	
		US Army Electronics Command Fort Monmouth, New Jersey	
13. ABSTRACT			
<p>The objective of this study was to demonstrate the extent to which a difference in temperature (ΔT) between two levels near the ground (static atmospheric stability) and the ratio z/L (dynamic atmospheric stability) is related to other parameters indicative of turbulence and diffusion. The data show, if we assume that the rate of diffusion is determined by the intensity of turbulence, that (ΔT) measured through a shallow layer near the ground is not a good indicator of diffusion rates, particularly when the atmosphere is statically unstable. The ratio z/L does not appear to be a significantly better indicator for defining atmospheric stability than (ΔT) during highly unstable conditions.</p>			

DD FORM 1473

REPLACES DD FORM 1473, 1 JAN 64, WHICH IS OBSOLETE FOR ARMY USE.

UNCLASSIFIED

Security Classification

Ia

UNCLASSIFIED

Security Classification

14.	KEY WORDS	LINK A		LINK B		LINK C	
		ROLE	WT	ROLE	WT	ROLE	WT
	1. Turbulence 2. Similarity Theory 3. T-Array 4. Correlation Data						

TK

UNCLASSIFIED

Security Classification

Reports Control Symbol
OSD-1366

Technical Report ECOM-5468

CHARACTERISTICS OF THE TURBULENT DIFFUSION PARAMETERS
AS RELATED TO STABILITY

BY

Manuel Armendariz

James R. Scoggins
Texas A & M University

Atmospheric Sciences Laboratory
White Sands Missile Range, New Mexico

November 1972

DA Task No. IT061102B53A-17

Approved for public release; distribution unlimited.

U. S. Army Electronics Command
Fort Monmouth, New Jersey

IC

CONTENTS

	Page
INTRODUCTION	1
DISCUSSION	1
SOME FUNDAMENTAL CONCEPTS	2
Wind and its Variability	2
Definition of Turbulence	2
Factors Responsible for Turbulence	3
Diffusion Theory	6
Meteorological Variables Related to Diffusion Parameters	8
DATA	9
OBSERVED RELATIONSHIPS BETWEEN STATIC STABILITY AND SELECTED DIFFUSION PARAMETERS	9
Intensity of Turbulence	11
Variability of Wind Direction	14
Wind Speed	16
CONCLUSIONS	16
For the Layer 1.5 - 4.0 Meters	16
For the Layer 4.0 - 16.0 Meters	22
Wind Speed vs Stability	22
Relationship Between z/L and ΔT	22
Stability vs Diffusion Rates	22
LITERATURE CITED	23

INTRODUCTION

This study was undertaken at the request of the Selected Systems Effectiveness Program (SSEP) of the Joint Technical Coordinating Group for Munitions Effectiveness (JTCE/ME). The study is an effort to determine the effectiveness of present Department of Defense methodology in determining or predicting the diffusion of chemicals and/or radiological matter in the atmosphere. In particular, the study shows the extent to which a difference in temperature between two levels near the ground (static stability) or dynamic stability (ratio z/L) is related to the governing parameters of turbulence in the diffusion models considered.

DISCUSSION

Haugen and Fuquay [] pointed out that one should consider several meteorological parameters in characterizing the diffusive power of the atmosphere. Among these parameters are the following:

1. The mean wind velocity, determining the path of the cloud downwind from the source and the distribution of particles along the mean wind path. In the case of a continuous source this downwind transport results in a lower concentration of particles as the mean wind increases.
2. The RMS (standard deviation) of the wind direction (σ_A), determining the shape and distortion of the cloud, and in a sense serving as an indication of horizontal mixing.
3. The RMS (standard deviation) of the vertical wind direction (σ_E), determining the dispersion of the cloud in the vertical.
4. The vertical temperature gradient (ΔT) as an indicator of vertical mixing. If the temperature increases with height, the vertical mixing is limited to mechanical turbulence transport, whereas both mechanical and convective mixing generally occur during non-inversion conditions.

Relationships between the four parameters discussed above have been examined by Haugen and Fuquay [1] and Record et al. [2]. Models which quantitatively predict turbulent diffusion often assume that these relationships exist. In particular, the United States Army Combat Development Command's Field Manual 3-10, "Employment of Chemical and Biological Agents," utilizes a ΔT between heights of 0.5 and 4.0 meters to determine the horizontal and vertical rates of turbulent mixing. Various levels have been used for the measurement of the temperature gradient; e.g., project Ocean Breeze and Dry Gulch [1] used temperatures at heights of 2 and 17 meters. More recently, Record et al. [2] used heights of approximately 3 and 20 meters. The actual levels at which these temperature measurements were made were based primarily on existing instrumentation

at the site. Because of the highly varying conditions observed near the surface, there is a need to investigate the effects of choice of heights on turbulent diffusion parameters.

SOME FUNDAMENTAL CONCEPTS

A. Wind and Its Variability

Wind is initiated by pressure forces which are created by density gradients resulting from differential heating. It is modified by the rotation of the earth, frictional effects, and by centrifugal forces due to the curvature of the air trajectory. In the surface boundary layer curvature and coriolis effects often may be neglected. The speed and direction of the wind then depends primarily on the magnitude and direction of the pressure gradient force, and on the properties of the surface which determine the magnitude of the frictional force.

The influence of friction decreases with altitude and may vary with horizontal distance. When the surface is rough, the wind speed increases rapidly at heights just a few meters above the ground and less rapidly at greater heights. When the ground is smooth, the increase of wind speed with height is less pronounced but is still greater in the lowest few meters. Mechanical turbulence created by roughness elements decreases with height more rapidly over a rough surface than a smooth surface. When the degree of surface roughness changes horizontally, changes in wind and the intensity of turbulence at a given height result. Surface features such as hillocks, vegetation, and changes in other terrain features such as soil composition (which may lead to differential heating and variations in the pressure gradient force) induce spatial variations in wind speed and turbulence.

At present, it is not possible to determine analytically the micro- and mesoscale forces in space and time which affect the wind. It is possible, however, to determine the average magnitude of the forces in space, and hence the average wind may be determined with reasonable accuracy. Variations in the wind in both space and time within local areas are usually determined statistically, leaving much to be desired in terms of accuracy. It is this variability in wind which leads to extreme complexities in problems of diffusion and transport of airborne substances, impact predictions of unguided rockets, and numerous and varied meteorological problems, such as heat and momentum transfer and the coupling actions between layers of the atmosphere with differing wind speeds and stability.

B. Definition of Turbulence

The vector wind can be written as

$$\vec{V} = \vec{\bar{V}} + \vec{v}' \quad (1)$$

where the bar denotes an average value, an arrow a vector quantity (the absence of an arrow denotes a scalar quantity), and the prime a deviation from the average. Equation (1) may be written in component form as

$$u = \bar{u} + u'$$

$$v = \bar{v} + v' \quad (2)$$

$$w = \bar{w} + w'$$

where u , v , and w refer to the components of the wind along the orthogonal axes x , y , and z , respectively. Deviations from the average are referred to as turbulence and represent that portion of the wind which must be treated statistically. The average may or may not be a function of time. A hypothetical time trace of wind speed showing u and u' at a given location near the ground is illustrated in Figure 1. The variations in speed are caused by variations in the forces discussed above.

C. Factors Responsible for Turbulence

A convenient way of looking at the rate of growth and decay of turbulent energy is to examine the terms in the eddy kinetic energy equation. Lumley and Panofsky [3] wrote this equation in the simplified form

$$\begin{array}{cccc} \text{(A)} & \text{(B)} & \text{(C)} & \text{(D)} \\ \frac{D(\overline{KE'})}{Dt} = \bar{\rho} K_m \left(\left| \frac{\partial \bar{\mathbf{V}}}{\partial z} \right|^2 \right) & - & K_H \frac{\bar{\rho} g}{\bar{\theta}} \frac{\partial \bar{\theta}}{\partial z} & - \epsilon \end{array} \quad (3)$$

Here $(\overline{KE'})$ is the average kinetic energy of the three components of turbulence, K_H and K_m are the eddy exchange coefficients for heat and momentum, respectively, $\bar{\theta}$ is an average potential temperature in degrees Kelvin, $\bar{\rho}$ is an average density, g is gravity, $\bar{\mathbf{V}}$ is the mean wind velocity, z is height, and ϵ represents the dissipation of mechanical energy into heat. The terms comprising this equation are interpreted as follows:

1. Term (A) represents the time-rate-of-change of the average turbulent energy following the mean motion. Under equilibrium conditions and neglecting any advective processes, this term will be zero. A positive value of term (A) represents the growth and a negative value the decay of turbulent energy.

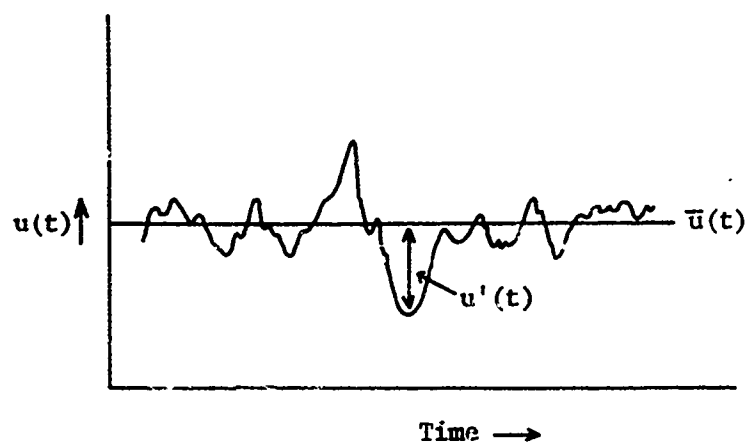


Figure 1. TIME TRACE OF WIND SPEED SHOWING
 $\bar{u}(t)$, $u(t)$, AND $u'(t)$.

2. Term (B) represents the work done by the turbulent stresses against the rates of mean strain. This term is usually positive and thus contributes to the growth of turbulent energy.

3. Term (C) represents the work done against buoyancy. This term can be an energy source or sink depending on the gradient of potential temperature, and it may be negligible when the gradient vanishes.

4. Term (D) represents the rate of dissipation of turbulent kinetic energy. Since dissipation is always a positive quantity, the negative sign makes the entire term an energy sink.

Richardson (see Sutton [4]) postulated that the state of turbulence can be determined from the ratio of term C to term B in Eq. (3), viz.,

$$R_f = \frac{K_H}{K_M} \frac{g}{\theta} \frac{\partial \bar{\theta} / \partial z}{(|\partial \bar{V} / \partial z|)^2} \quad (4)$$

R_f is referred to as the flux Richardson number. If it is assumed that $K_H/K_M = 1$, then Eq. (4) becomes the gradient Richardson number, R_i . If $R_f = 1$, then the buoyancy forces remove turbulent energy at the same rate that it is being produced by the shearing stresses. This does not mean that $R_f = 1$ is a critical value for predicting the onset of turbulent motion but rather the condition for equilibrium. It is clear, however, that $R_f < 1$ indicates turbulent energy growth and $R_f > 1$ indicates decay.

It is also possible to express R_f as a function of height in non-dimensional form using similarity theory [3]. A non-dimensional wind shear, S , can be defined as

$$S \equiv \frac{kz}{u^*} \frac{\partial \bar{V}}{\partial z} \quad (5)$$

where k is von Karman's constant, u^* is the friction velocity, and the other variables are as previously defined. A scaling length, L , defined by Monin and Obukhov (see Lumley and Panofsky [3]), is given by

$$L \equiv - \frac{C_p \rho \bar{\theta} u^{*3}}{kgH} \quad (6)$$

where C_p is the specific heat of air at constant pressure, and H is the vertical flux of heat. Using Eqs. (4), (5), and (6) and the following expressions for H and K_M :

$$H \equiv - \rho C_p K_H \frac{\partial \bar{\theta}}{\partial z} \quad (7)$$

$$K_m \equiv u^{*2} / \frac{\partial v}{\partial z}$$

we arrive at

$$SRf = \frac{-gHkz}{C_p \bar{\rho} u^{*3}} = z/L \quad (8)$$

Observation has shown [3] that in near-neutral conditions $S \doteq 1$ so that $Rf \doteq z/L$. Hence, z/L is a measure of dynamic stability and thereby is a means of ascertaining whether or not there is a growth or decay of turbulent kinetic energy.

D. Diffusion Theory

The intensity of turbulence, I , is given by Slade [5] as

$$I_x = \frac{\sigma_u}{\bar{V}}; \quad I_y = \frac{\sigma_v}{\bar{V}}; \quad I_z = \frac{\sigma_w}{\bar{V}} \quad (9)$$

where the σ 's represent the standard deviation of the longitudinal (u), lateral (v), and vertical (w) components of turbulence, \bar{V} is the average wind speed, and x , y , and z refer to coordinate directions. Longitudinal refers to the direction along the mean wind, and lateral to the perpendicular to the mean wind direction. The diffusing power of the atmosphere is directly related to the I 's. When the average wind direction is along the x -axis such that $\bar{v} = 0$, then there is no y component and we can write

$$\sigma_A = \frac{\sigma_v}{\bar{V}} \quad \text{and} \quad \sigma_\phi = \frac{\sigma_w}{\bar{V}} \quad (10)$$

where A is wind direction (azimuth) in radians, and σ_ϕ is the standard deviation of the inclination of the vector wind in radians (when $\phi = 0$, the wind is horizontal). In practical diffusion work the basic problem is to relate the measurable quantities given in Eqs. (9) and (10) to the dispersion of airborne effluents under various stability conditions.

Statistical theories of turbulent diffusion show that the variance of particle diffusion in the y-direction under different conditions is given by [6]

$$\overline{y^2(t)} = 2Kt \quad (t \text{ large}) \quad (11)$$

$$\overline{y^2(t)} = \overline{v'^2} t^2 \quad (t \text{ small}) \quad (12)$$

and

$$\overline{y^2(t)} = 1/2 C_y^2 \overline{u^2} t^{2-n} \quad (t \text{ intermediate}) \quad (13)$$

where Gaussian distribution of the particles has been assumed, and where

$y(t)$ = cross wind distance that a particle moves
from some origin

K = eddy diffusion coefficient

t = time

C_y = eddy diffusion parameter in the y-direction

n = stability parameter

v' = crosswind turbulent fluctuation

u = mean wind speed

The constant K in Eq. (11) and C_y in Eq. (13) depend upon the intensity of turbulence as given in Eqs. (9) and (10). While it will not be shown here, the value of $\overline{y^2(t)}$ in Eq. (12) depends on the total spectrum of the turbulence. In Eq. (13), D_y^2 is a function of the average wind speed, the variance of the lateral velocity fluctuations, and stability. The influence of stability is contained in the parameter n defined from the wind profile by the relation

$$\frac{\bar{V}_1}{\bar{V}_2} = \left(\frac{z_1}{z_2} \right)^{\frac{n}{2-n}} \quad (14)$$

where \bar{V}_1 is measured at z_1 and \bar{V}_2 at z_2 . Different values of n represent different stability conditions. Thus, the value of $\frac{n}{2-n}$ in Eqs. (11) - (13), which determines the distribution of particles in the cross-wind direction (along the y -axis), is related to the intensity of turbulence given by Eq. (9), the total energy spectrum of turbulence, variability of wind direction (Eq. (10)), stability, and average wind speed. As discussed previously, these variables are interrelated with each one usually expressed as a function of stability. Thus, the rate of diffusion is related to the degree of stability.

E. Meteorological Variables Related to Diffusion Parameters

The meteorological variables most commonly related to atmospheric diffusion near the ground include: 1) the intensity of turbulence, 2) the spectrum of turbulence, 3) variability of wind direction (vertical and horizontal), 4) stability, and 5) wind speed. These parameters are related in some way to K and C_y in Eqs. (11) and (13), or to the production terms in the kinetic energy equation for turbulence (Eq. (3)). Static stability and wind speed near the ground are related through Eq. (14). To illustrate the relationship between stability and the diffusion coefficients, the following data were taken from page 243 of Atmospheric Diffusion by Pasquill [7].

TABLE 1. DIFFUSION PARAMETERS VS. ATMOSPHERIC STABILITY

Stability	$T_{183 \text{ ft}} - T_{15 \text{ ft}} (^{\circ}\text{F})$	n	$C_y (\text{m}^{n/2})$
Neutral	-1 and 0	0.25	0.095-0.14
Moderate inversion	+1 to +5	0.35	0.052-0.077
Strong Inversion	6	0.50	0.029-0.074

The diffusion coefficient in the lateral direction, C_y , is assumed to equal that in the vertical direction. Static stability is a function of wind speed, terrain conditions, the type of air mass present, cloudiness (or radiation), and other parameters. It is observed that the concentration of pollutants increases over cities during stable conditions while rapid dispersion takes place during unstable conditions. While the magnitude of the diffusion coefficient is proportional to instability, the relationship between the concentration of pollutants and stability conditions does not always exist. For example, mechanical turbulence may exist even during inversion conditions, which leads to an increase in C_y . A wide range of values for the diffusion coefficients under different atmospheric conditions are summarized by Pasquill [7] and Gifford [6]. A rather wide range of values has been obtained from experimental results.

DATA

The data utilized in this study were obtained from instruments set up in an array forming a "T" over distances of 300 meters. The instruments utilized were R. M. Young Company's UVW (propeller anemometers) along with unspirated thin wire thermocouples. The accuracies of these instruments and data, spacing of poles on which instruments were mounted, and terrain characteristics have been described by Armendariz et al. [8]. Briefly, the area is composed of hillocks 2 to 3 meters in height and randomly spaced approximately 5 to 10 meters apart. The distance constant of the wind instruments is 1.3 meters and data were automatically collected at a rate of one sample per second. The thermocouples, .0025 cm in diameter and made of copper constantan, have a time constant less than 0.5 seconds. Wind instruments were placed at 1.5 and 4.0, or 4.0 and 16.0 meters in height on alternate poles in the array. Temperature differences were recorded between 0.5 and 4.0 meters and between 4.0 and 16.0 meters. Data were collected during the months of January, February, and March of 1970. In general, the collection of data was made over two-hour periods during both day and night. There were some periods of continuous data collection lasting six or seven hours.

OBSERVED RELATIONSHIPS BETWEEN STATIC STABILITY AND SELECTED DIFFUSION PARAMETERS

Relationships between meteorological variables such as static stability, variations in wind direction, wind speed, etc., and atmospheric diffusion parameters are complicated even in relatively simple situations, and cannot be specified with confidence in complex situations. The analysis of the T-array data presented here is aimed at illustrating some of the complexities involved as well as some of the relationships between static stability represented as the difference in temperature between two heights and certain parameters associated with atmospheric diffusion. The objective is to demonstrate, for the period of study chosen, the extent to which a difference

in temperature between two levels near the ground and the ratio z/L are related to other parameters indicative of turbulence and diffusion.

A. Intensity of Turbulence

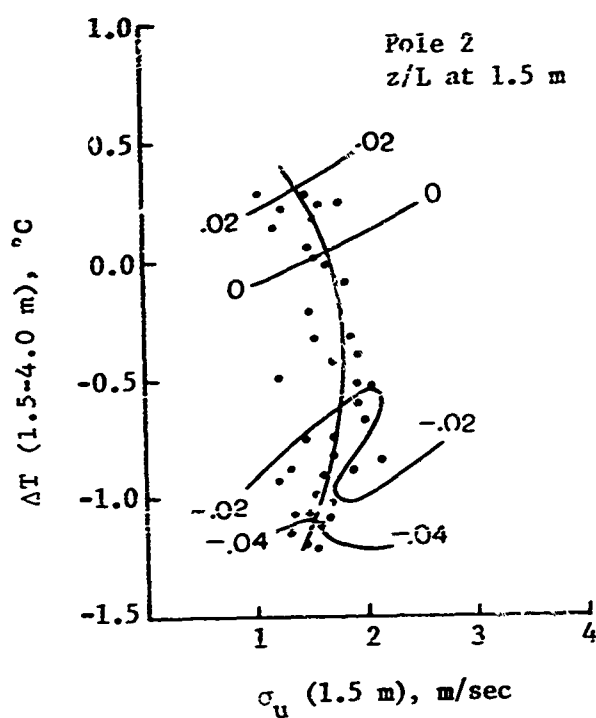
1. Longitudinal -- The longitudinal intensity of turbulence is represented by σ_u , which is the standard deviation of the fluctuation along the mean wind flow. The relationships between z/L , ΔT , and σ_u for selected heights are shown in Figure 2. The difference in temperature between the indicated heights in each figure is shown on the ordinate, σ_u on the abscissa, while z/L is the third variable plotted in each figure. Isopleths are drawn for values of z/L , and a line was drawn by eye to represent the relationship between ΔT and σ_u .

In Figure 2a, σ_u is a function of ΔT but the relationship is not linear. It can be seen that σ_u initially increases as ΔT decreases, but then decreases as ΔT decreases further. The ratio z/L decreases as ΔT decreases, but the decrease is not regular when z/L becomes less than approximately -0.02. In Figure 2a neither ΔT nor z/L is a good indicator of σ_u , which as we recall from the theory presented in Section II is directly related to the diffusive power of the atmosphere for a given mean wind speed. Figure 2b differs from Figure 2a only in that z/L and σ_u are computed at a height of 4 meters rather than 1.5 meters. The results are similar and show some indication of a slight increase in σ_u with a decrease in ΔT . As in Figure 2a, there is a poor relationship between z/L and σ_u when z/L becomes negative (less than -0.05).

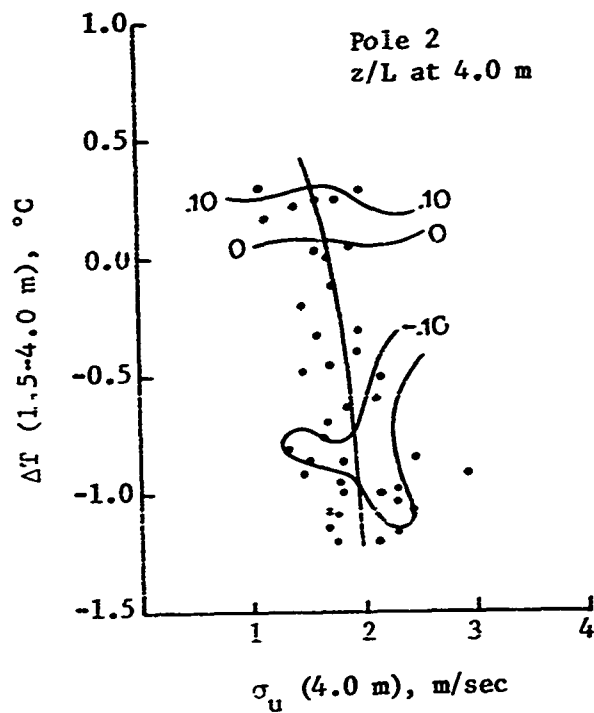
In Figure 2c, where ΔT is determined between 4 and 16 meters, and z/L and σ_u at 4 meters, σ_u is related to ΔT except when ΔT is large and negative. The ratio z/L decreases as ΔT decreases and σ_u increases except at large negative ΔT . When ΔT reaches values of -0.5 and less it no longer indicates the level of turbulence. In this range, z/L increases as σ_u increases. When ΔT exceeds -0.3, both ΔT and z/L are related to σ_u .

The fact that relationships between the parameters considered here change drastically at different levels in the atmosphere is illustrated in Figure 2d. This figure is similar to Figure 2c with the only change being that z/L and σ_u are determined at 16 meters rather than at 4 meters. In Figure 2d, σ_u increases as ΔT decreases, but for any ΔT , σ_u may vary from approximately 1.5 to 3 mps. The relationship between ΔT and σ_u is quite weak. z/L and ΔT show a similar relationship to σ_u .

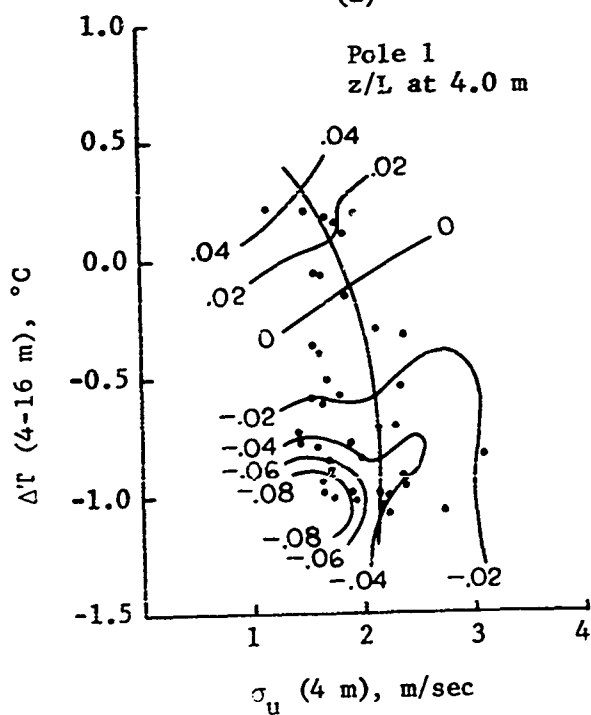
2. Lateral -- In Figure 3 the lateral intensity of turbulence, σ_v , is shown as a function of z/L and ΔT for the same data as in Figure 2. The relationships between the variables in Figure 3a are the same as those discussed above for Figure 2a. By comparison, Figure 3b differs considerably from its counterpart, Figure 2b. Here, σ_v decreases with decreasing ΔT when $\Delta T < -0.5$. As ΔT becomes smaller, σ_v varies by a factor



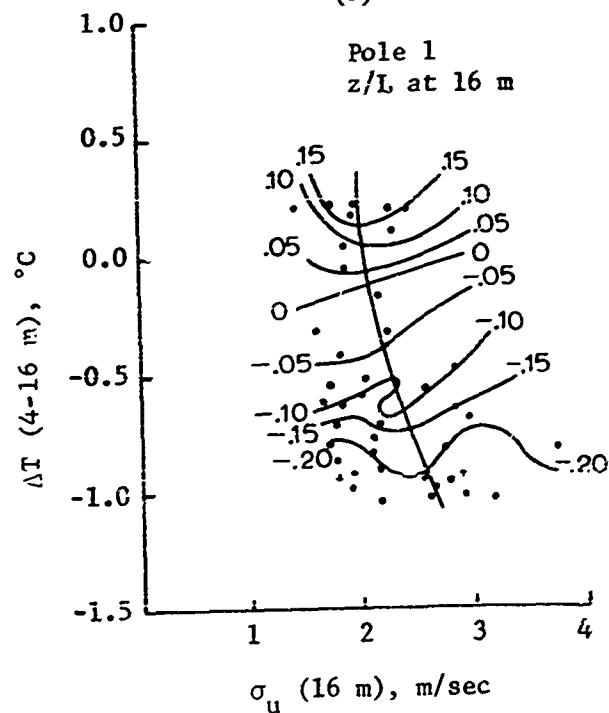
(a)



(b)

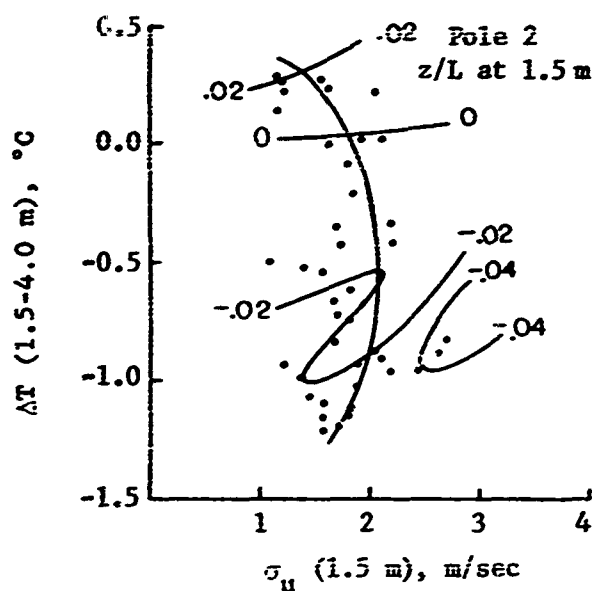


(c)

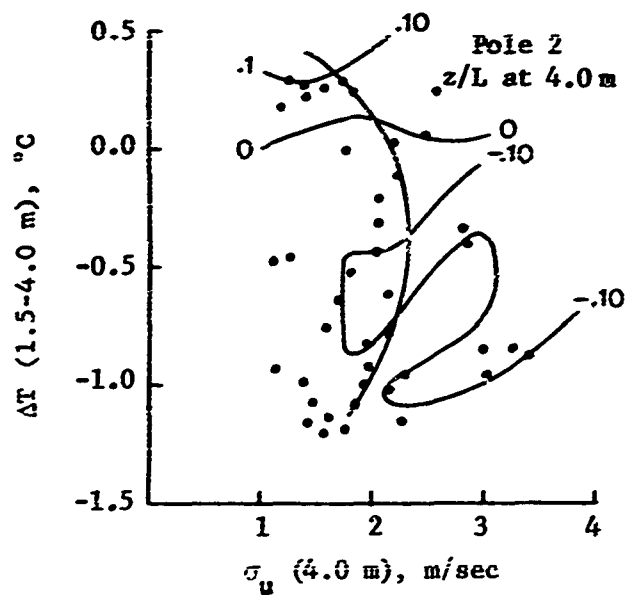


(d)

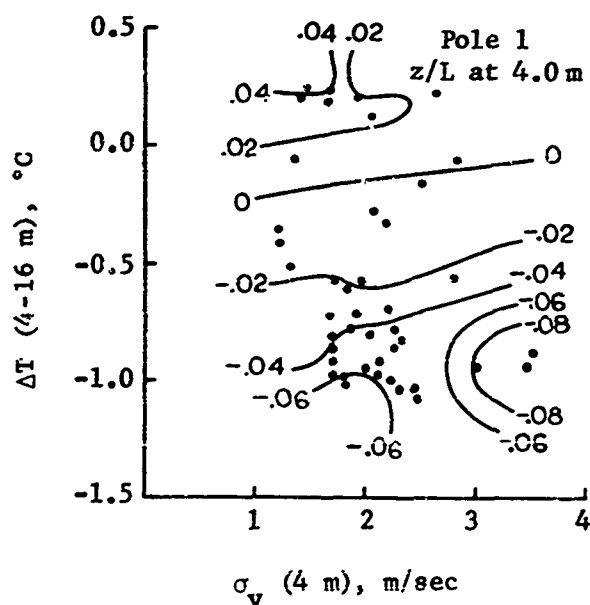
Figure 2. GRAPHICAL RELATIONSHIPS BETWEEN ΔT , σ_u , AND z/L .



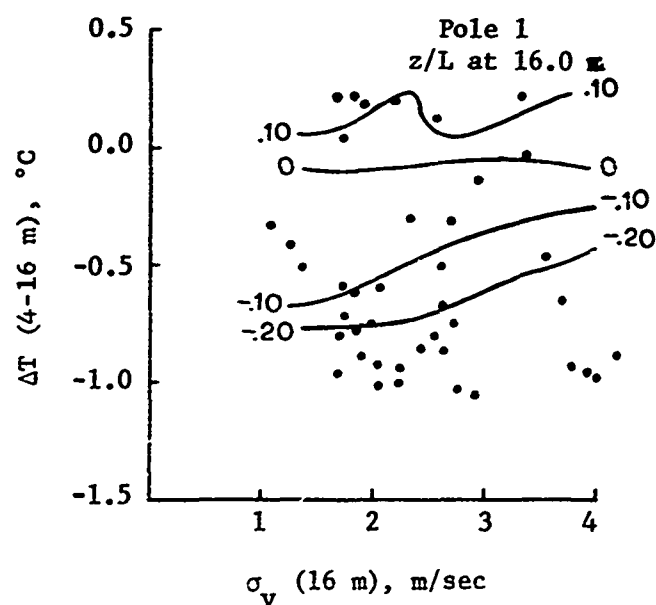
(a)



(b)



(c)



(d)

Figure 3. GRAPHICAL RELATIONSHIPS BETWEEN ΔT , σ_v , AND z/L .

of 2-3 for a given value of ΔT . Except for near-neutral conditions, z/L is not a good indicator of σ_v and when $z/L < -0.1$, the relationship between z/L and σ_v apparently has vanished.

In Figure 3c, ΔT is not related to σ_v . σ_v varies from approximately 1.5 to 3.5 for any value of ΔT . The ratio z/L also is not related to σ_v any better than to ΔT . These rather poor relationships extend to Figure 3d, which shows that σ_v is not related to ΔT and that σ_v varies between 1 and 4 mps for any given value of ΔT . In addition, there is no apparent relationship between z/L and σ_v .

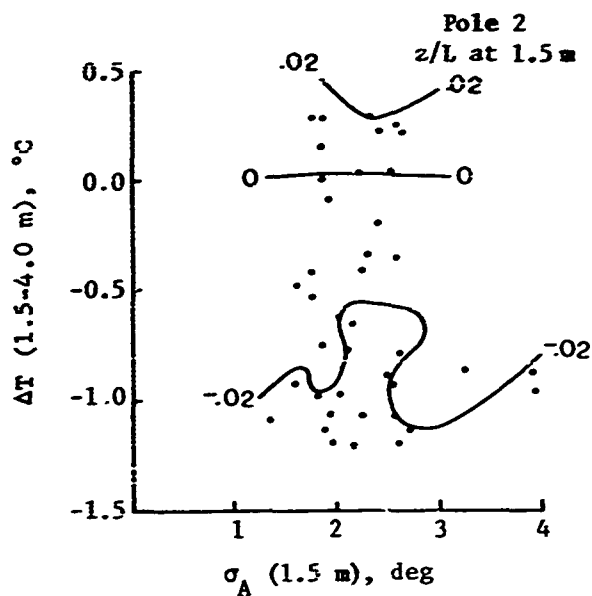
3. Vertical -- Relationships between z/L , ΔT , and σ_w are shown in Figure 4. Conditions represented in this figure are similar to those in Figures 2 and 3. In Figure 4a, σ_w is a function of $\Delta T > 0$. When ΔT is less than this value, σ_w does not depend upon ΔT . The intensity of the vertical component of turbulence, σ_w , increases as z/L decreases to values near -0.02, but below this value z/L and σ_w are essentially constant. Figure 4b is similar to Figure 4a and shows that σ_w increases with a decrease in $\Delta T > -0.4$, and decreases for smaller values of ΔT . In this figure, z/L is a poor indicator of σ_w for all values.

Figure 4c is somewhat similar to Figures 4a and b and shows σ_w to be related to ΔT , but the relationship is not linear. σ_w increases as ΔT decreases to values above about -0.3, but as ΔT becomes smaller σ_w remains essentially constant, with some slight tendency to decrease as ΔT approaches -1.0. The ratio z/L decreases with an increase in σ_w for all ΔT except for $\Delta T < -0.8$, in which case larger negative values of z/L are associated with smaller values of σ_w .

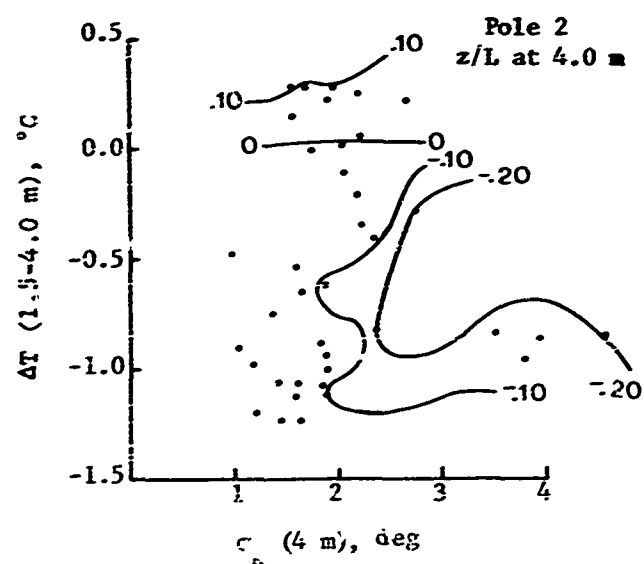
Figure 4d differs from Figures 4a-c in that σ_w increases as ΔT decreases throughout the entire range of ΔT . In addition, z/L decreases as σ_w increases and ΔT decreases. In this figure, both ΔT and z/L are related to σ_w in a reasonably definite way.

B. Variability of Wind Direction

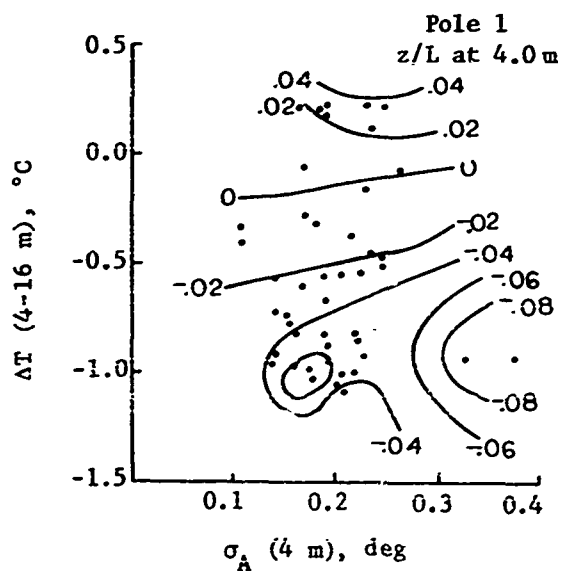
The variability of wind direction is considered in Figure 5. The conditions in this figure are similar to those in Figures 2-4 except that the standard deviation of component wind speeds has been replaced by σ_A . As we can see from Eq. (10), σ_A is a measure of the intensity of turbulence for a given mean wind speed. In Figure 5a, σ_A is not related to ΔT ; in addition, z/L is not related to σ_A in any definite way. When $z/L < -0.02$, σ_A may vary by a factor of about 4 while z/L remains essentially constant. Similar relationships are observed in Figure 5b except that when z/L becomes < -0.1 , larger values of σ_A are associated with smaller values of z/L .



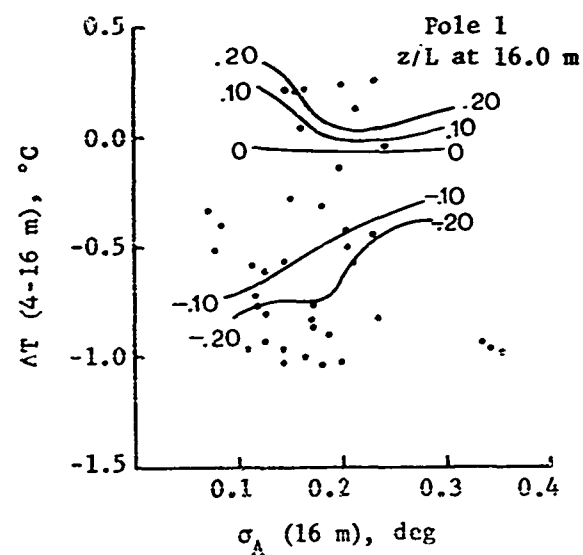
(a)



(b)

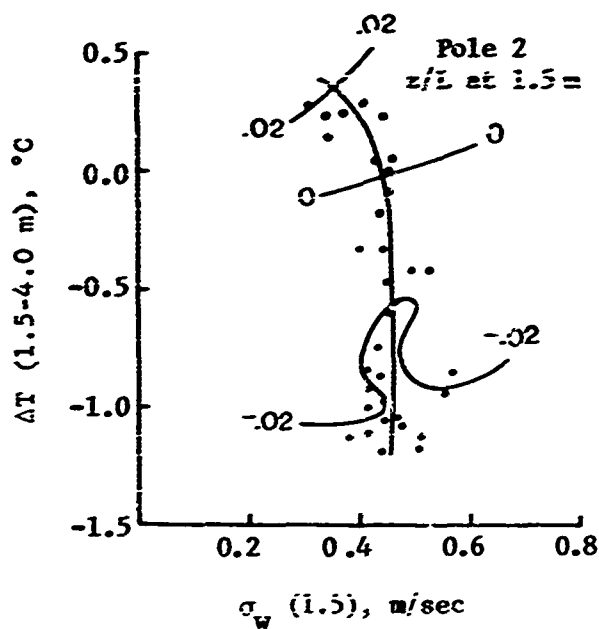


(c)

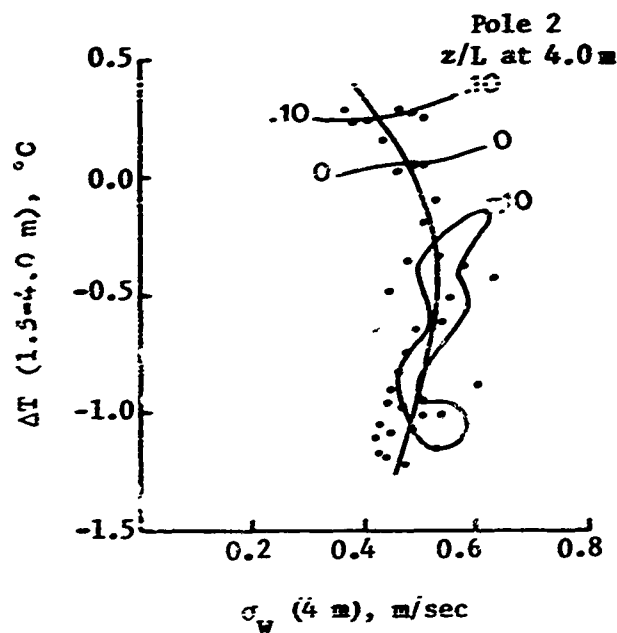


(d)

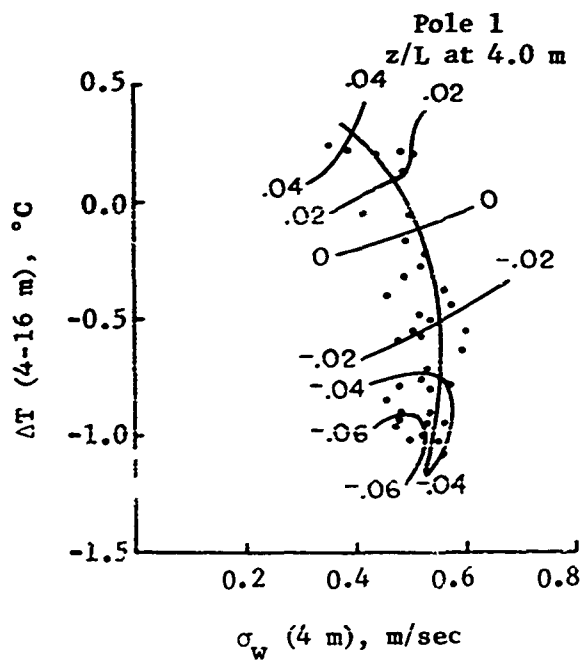
Figure 5. GRAPHICAL RELATIONSHIPS BETWEEN ΔT , σ_A , AND z/L .



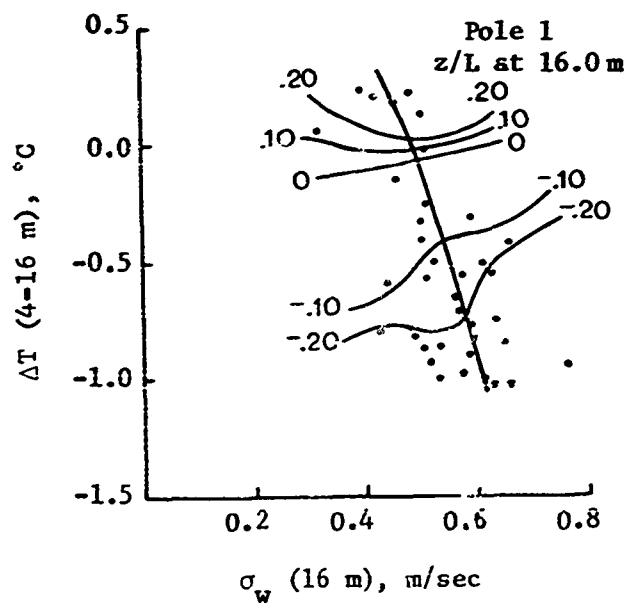
(a)



(b)



(c)



(d)

Figure 4. GRAPHICAL RELATIONSHIPS BETWEEN ΔT , σ_w , AND z/L .

Figure 5c is similar to Figure 5b. Again, σ_A is not a function of ΔT and is a function of z/L only when $z/L < -0.04$, which corresponds to a ΔT of approximately -0.80 . For $z/L < -0.04$, σ_A increases as z/L decreases. Thus, ΔT is not a good indicator of σ_A , while z/L is valid only at values ≥ 0.04 . Similar relationships are observed in Figure 5d except that when z/L approaches -0.1 , σ_A tends to increase as z/L decreases.

Figures 6a and 6b show σ_A at 1.5 meters versus ΔT between 0.5 and 4.0 meters and 1.5 and 4.0 meters for the period January-March 1970. Figure 6a differs considerably from Figure 6b with the difference due entirely to a slight change in the layer over which ΔT was measured. In excess of 150 hours of data are plotted in each part of these figures with each point representing a 15-minute average value. This larger sample of data agrees in general with the results from the much smaller sample considered in Figure 5. The major difference is that the range of σ_A for a given ΔT is much larger in Figures 6a and 6b than in Figure 5. Record et al. [2] found σ_A to vary with wind speed during stable and unstable conditions; however, this relationship was not examined.

From the above discussion it is evident that z/L and ΔT are somewhat related. Of course, they should be since ΔT appears in the Richardson number (Ri) and $z/L = Ri$ for near-neutral conditions. The experimental relationship is shown in Figure 7 for the period January-March 1970. The relationship is quite poor. The scatter when $|z/L|$ and $|\Delta T|$ are large suggests that, at most, one or possibly neither of these parameters can be used as an indicator of the level of turbulence. In principle, z/L should be the better indicator; however, some refinements in its computation may be necessary when atmospheric conditions vary greatly from neutral.

C. Wind Speed

The relationships between the longitudinal (\bar{u}) and lateral (\bar{v}) component wind speeds at 1.5 meters, and T between 0.5 - 4.0 and 1.5 - 4.0 meters, are shown in Figures 8a and 8b for the period January-March 1970. For both wind components, the average wind speed increases as ΔT decreases for $\Delta T > 0$. When $\Delta T < 0$, the functional dependence disappears. A line has been drawn by eye through the points on each part of the figure when $\Delta T > 0$. The range in wind speed for a given ΔT is large, particularly for the lateral component, but there is little doubt that a trend is present in the data when ΔT is positive.

CONCLUSIONS

A. For the Layer 1.5 - 4.0 Meters

The standard deviations of all three components of the wind vector at 1.5 and 4.0 meters (σ_u , σ_v , σ_w) generally increase with a decrease in ΔT

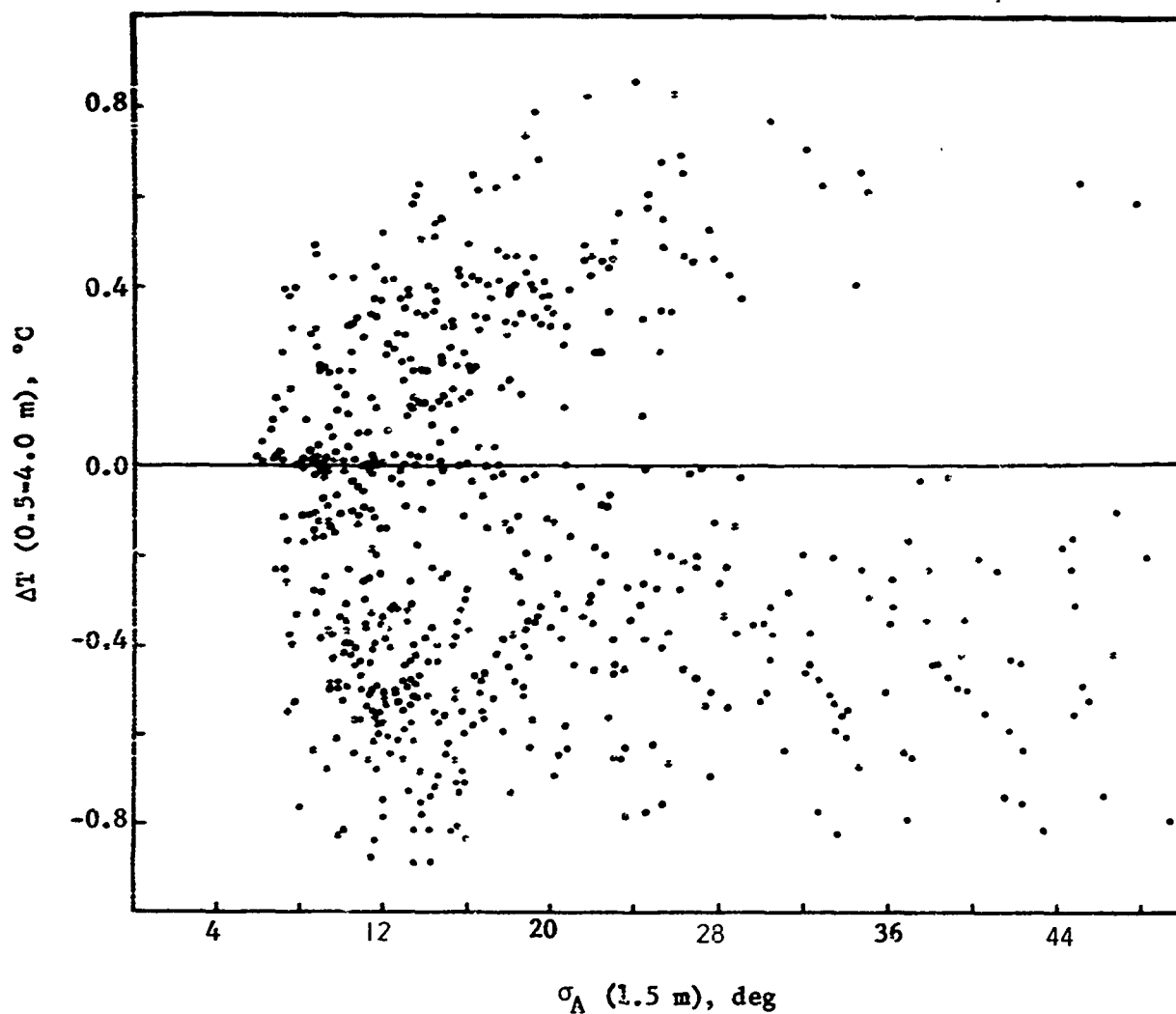


Figure 6(a). GRAPHICAL RELATIONSHIPS BETWEEN
 $\Delta T(0.5-4.0 \text{ m})$ AND σ_A .

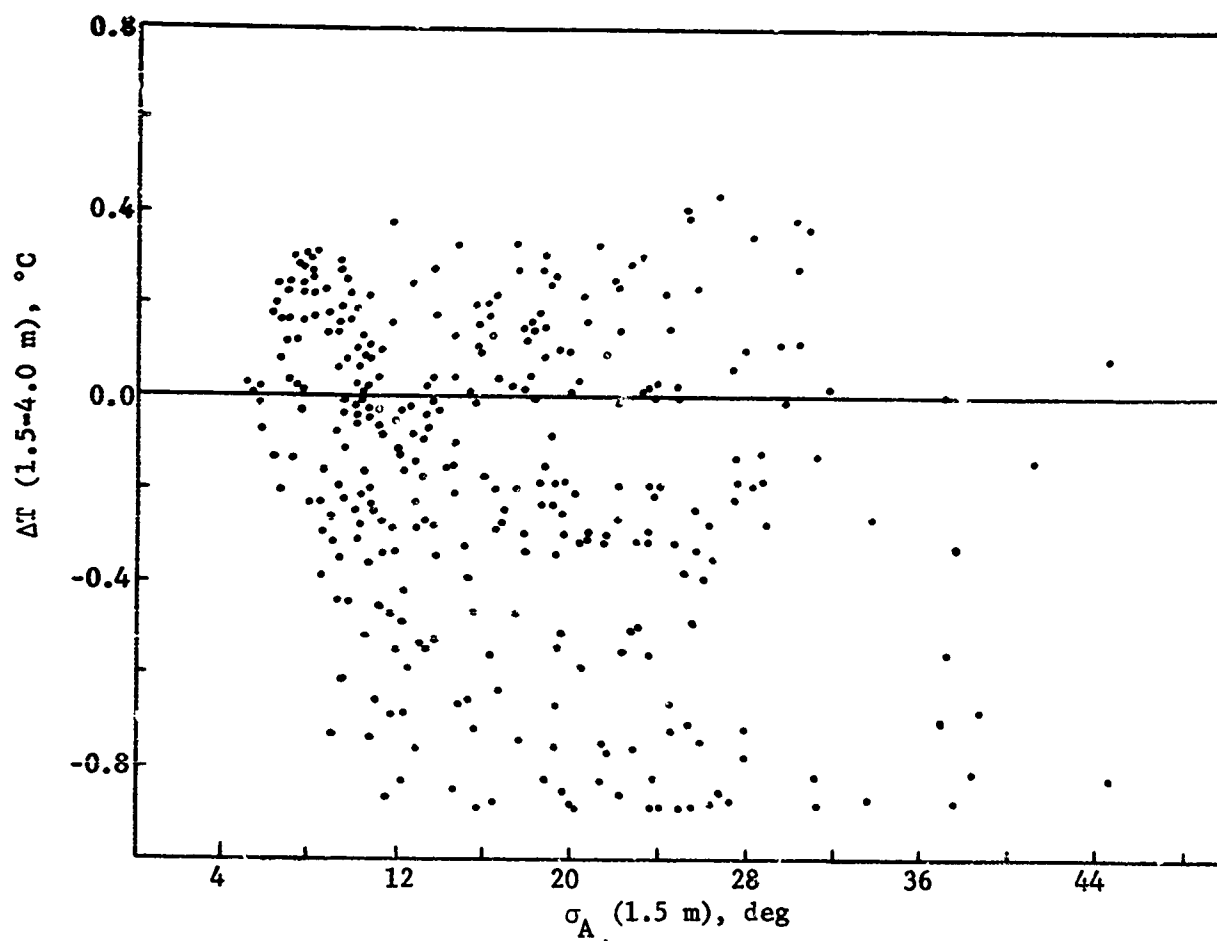


Figure 6(b). GRAPHICAL RELATIONSHIPS BETWEEN
 $\Delta T(1.5-4.0 \text{ m})$ AND σ_A .

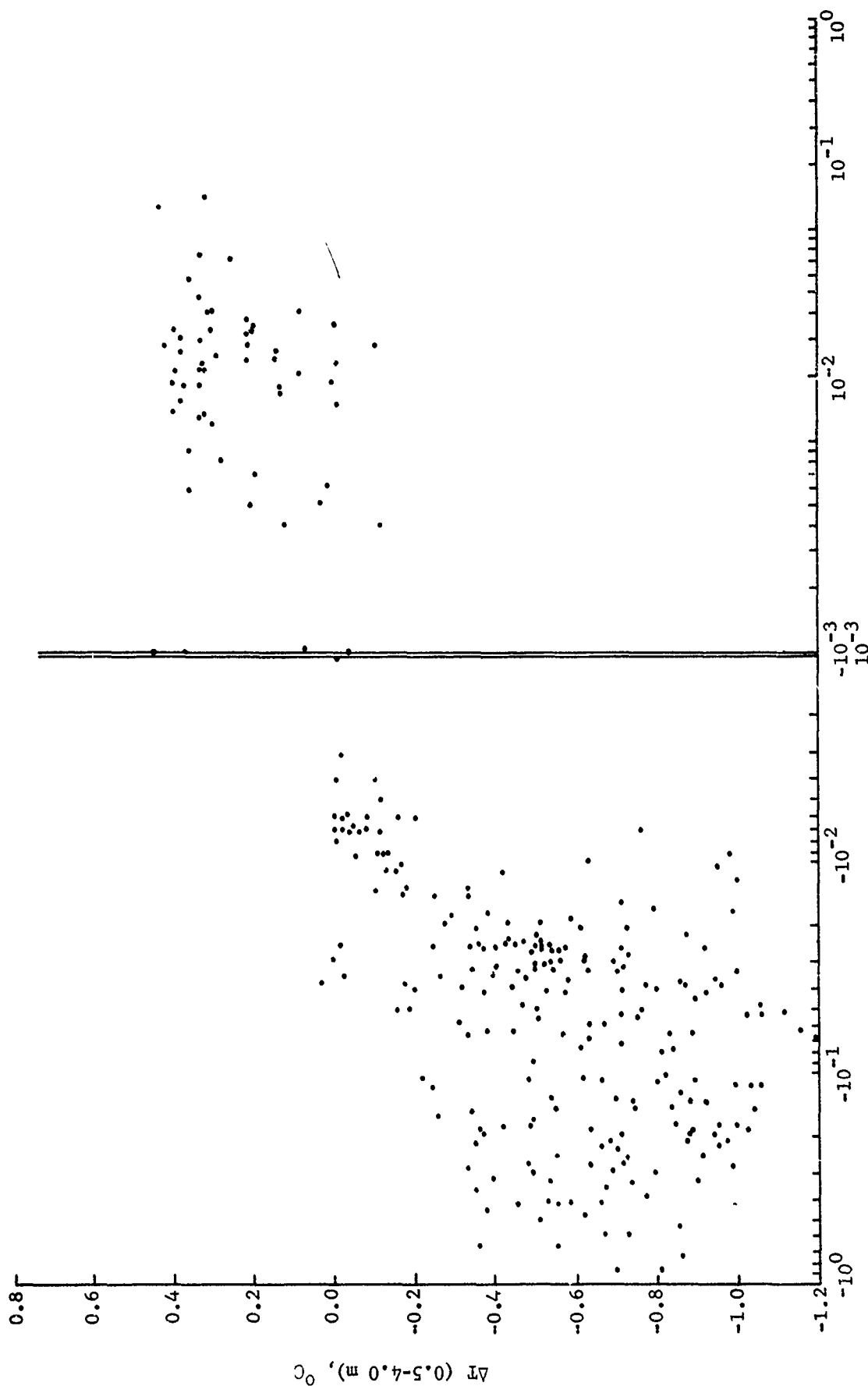


Figure 7. GRAPHICAL RELATIONSHIP BETWEEN ΔT AND z/L .
(THE DOUBLE LINE INDICATES A BREAK IN THE ABSCISSA.)

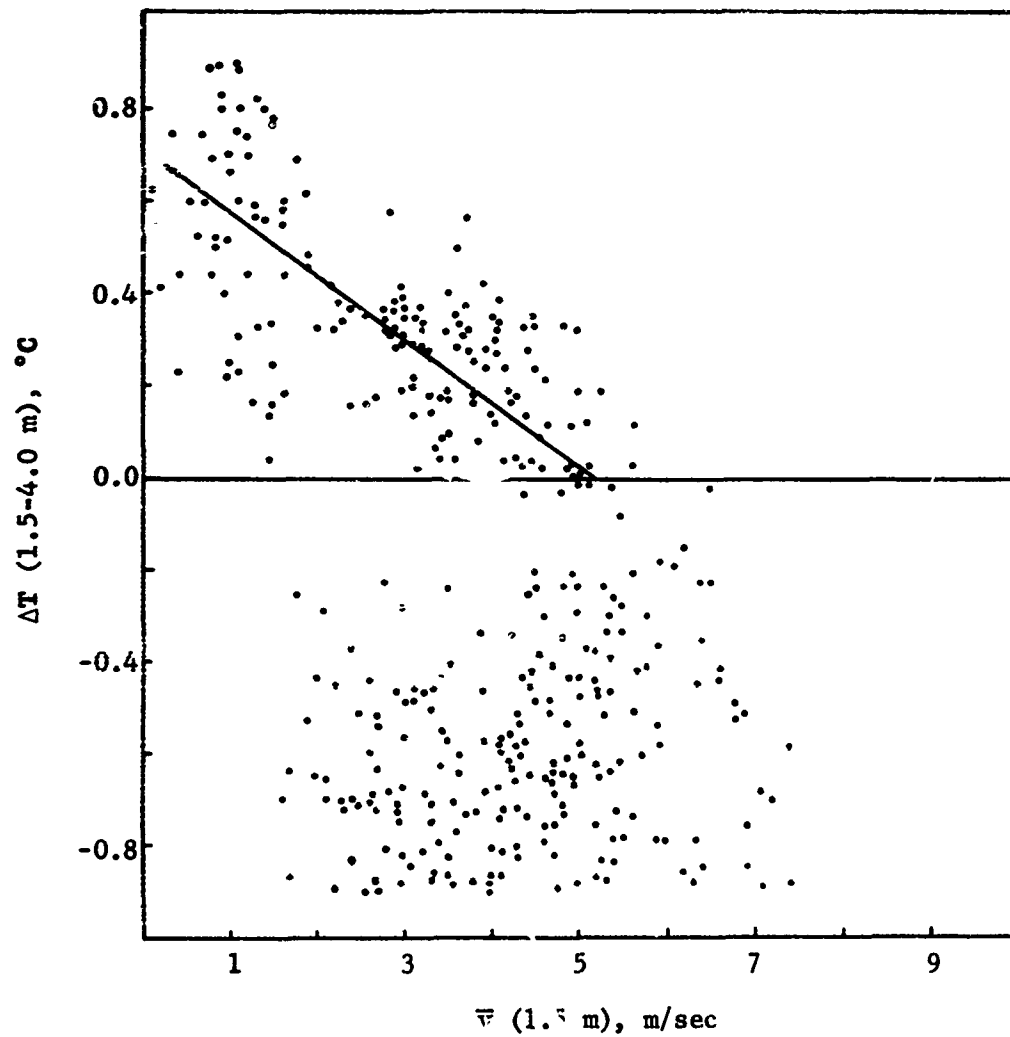


Figure 8(b). GRAPHICAL RELATIONSHIPS BETWEEN ΔT AND $\bar{V}(1.5 \text{ m})$.

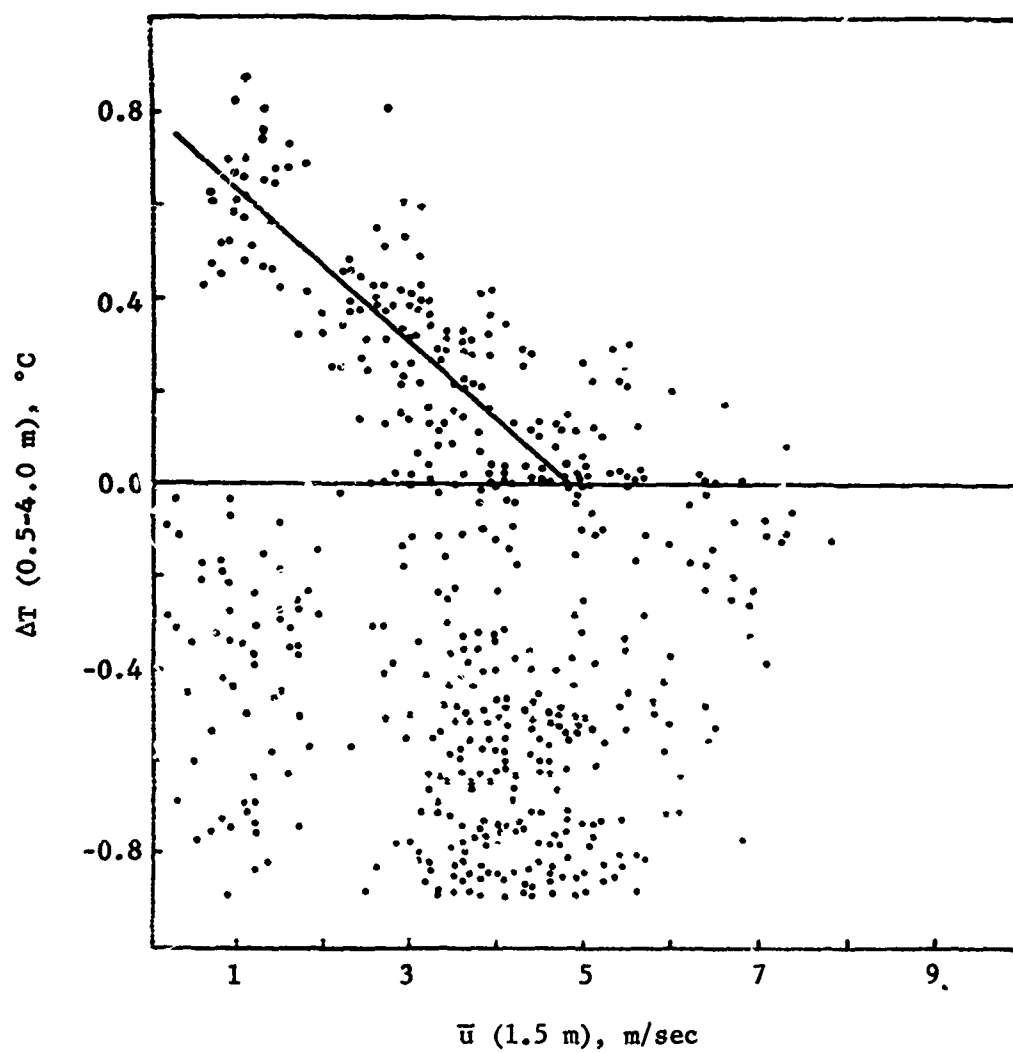


Figure 8(a). GRAPHICAL RELATIONSHIPS BETWEEN
 ΔT AND $\bar{u}(1.5 \text{ m})$.

(1.5 - 4.0 meters) when $\Delta T > -0.25^\circ\text{C}$, but when $\Delta T < -0.25^\circ\text{C}$, the magnitude of the σ 's generally becomes smaller as ΔT becomes more negative. z/L also decreases as the σ 's increase for values of $z/L > -0.02$, but for smaller values of z/L no general relationship appears to hold. The standard deviation of wind direction (σ_A) is not related to ΔT or z/L .

B. For the Layer 4.0 - 16.0 Meters

Standard deviations of the lateral component (σ_v) and wind direction (σ_A) are not related to ΔT or z/L for any range of values. The standard deviations of the longitudinal and vertical components (σ_u and σ_w) increase with a decrease in ΔT (4.0 - 16.0 meters) for $\Delta T > -0.25^\circ\text{C}$, but when $\Delta T < -0.25^\circ\text{C}$, the magnitude of the σ 's either remains constant or becomes smaller as ΔT becomes more negative. At the top of the layer (16.0 meters), σ_u and σ_w tend to increase with a decrease in ΔT although the relationship is poor.

C. Wind Speed vs Stability

The wind speed increases as the degree of static stability decreases, but only during stable conditions. During unstable conditions (decrease of temperature with height), the wind speed may vary from 1-8 m/sec and is independent of the degree of instability.

D. Relationship Between z/L and ΔT

z/L increases as ΔT increases in near-neutral conditions, but the relationship diminishes when the degree of stability is large or small.

E. Stability vs Diffusion Rates

If we assume that the rate of diffusion is determined by the intensity of turbulence (fluctuations about the mean), ΔT measured through a shallow layer near the ground is not a good indicator of diffusion rates, particularly when the atmosphere is statically unstable (ΔT negative). z/L does not appear to be a significantly better indicator than ΔT during highly unstable conditions.

LITERATURE CITED

1. Haugen, Duane A., and James J. Fuquay, 1963, "The Ocean Breeze and Dry Gulch Diffusion Programs," Vol. 1, AFCRL, 240 pp.
2. Record, R. A., R. N. Swanson, H. E. Cramer, and R. K. Dumbauld, 1970, "Analysis of Lower Atmospheric Data for Diffusion Studies," NASA CR-61327.
3. Lumley, John L., and Hans A. Panofsky, 1964, The Structure of Atmospheric Turbulence, John Wiley and Sons, 239 pp.
4. Sutton, O. G., 1953, Micrometeorology, McGraw-Hill Book Co., pp. 152-153.
5. Slade, David H., ed., 1968, Meteorology and Atomic Energy 1968, U. S. Atomic Energy Commission, Ch. 2.
6. Gifford, Frank A., 1968, Meteorology and Atomic Energy 1968, U. S. Atomic Energy Commission, Ch. 3.
7. Pasquill, F., 1962, Atmospheric Diffusion, D. Van Nostrand Co., Ltd., 297 pp.
8. Armendariz, M., L. J. Rider, G. S. Campbell, D. L. Favier, and Juana Serna, 1971, "Turbulence Measurements from a T-Array of Meteorological Sensors," ECOM-5362, Atmospheric Sciences Laboratory, U. S. Army Electronics Command, White Sands Missile Range, New Mexico, 869 pp.

ATMOSPHERIC SCIENCES RESEARCH PAPERS

1. Miers, B. T., and J. E. Morris, Mesospheric Winds Over Ascension Island in January, July 1970, ECOM-5312, AD 711851.
2. Webb, W. L., Electrical Structure of the D- and E-Region, July 1970, ECOM-5313, AD 714355.
3. Campbell, G. S., F. V. Hansen and R. A. Dise, Turbulence Data Derived from Measurements on the 32-Meter Tower Facility, White Sands Missile Range, New Mexico, July 1970, ECOM-5314, AD 711852.
4. Pries, T. H., Strong Surface Wind Gusts at Holloman AFB (March-May), July 1970, ECOM-5315, AD 711853.
5. D'Arcy, E. M., and B. F. Engebos, Wind Effects on Unguided Rockets Fired Near Maximum Range, July 1970, ECOM-5317, AD 711854.
6. Matonis, K., Evaluation of Tower Antenna Pedestal for Weather Radar Set AN/TPS-41, July 1970, ECOM-5317, AD 711520.
7. Monahan, H. H., and M. Armendariz, Gust Factor Variations with Height and Atmospheric Stability, August 1970, ECOM-5320, AD 711855.
8. Stenmark, E. B., and L. D. Drury, Micrometeorological Field Data from Davis, California; 1966-67 Runs Under Non-Advection Conditions, August 1970, ECOM-6051, AD 726390.
9. Stenmark, E. B., and L. D. Drury, Micrometeorological Field Data from Davis, California; 1966-67 Runs Under Advection Conditions, August 1970, ECOM-6052, AD 724612.
10. Stenmark, E. B., and L. D. Drury, Micrometeorological Field Data from Davis, California; 1967 Cooperative Field Experiment Runs, August 1970, ECOM-6053, AD 724613.
11. Rider, L. J., and M. Armendariz, Nocturnal Maximum Winds in the Planetary Boundary Layer at WSMR, August 1970, ECOM-5321, AD 712325.
12. Hansen, F. V., A Technique for Determining Vertical Gradients of Wind and Temperature for the Surface Boundary Layer, August 1970, ECOM-5324, AD 714366.
13. Hansen, F. V., An Examination of the Exponential Power Law in the Surface Boundary Layer, September 1970, ECOM-5326, AD 715349.
14. Miller, W. B., A. J. Blanco and L. E. T aylor, Impact Deflection Estimators from Single Wind Measurements, September 1970, ECOM-5328, AD 716993.
15. Duncan, L. D., and R. K. Walters, Editing Radiosonde Angular Data, September 1970, ECOM-5330, AD 715351.
16. Duncan, L. D., and W. J. Vechione, Vacuum Tube Launchers and Boosters, September 1970, ECOM-5331, AD 715350.
17. Stenmark, E. B., A Computer Method for Retrieving Information on Articles, Reports and Presentations, September 1970, ECOM-6050, AD 724611.
18. Hudlow, M., Weather Radar Investigation on the BOMEX, September 1970, ECOM-5329, AD 714191.
19. Combs, A., Analysis of Low-Level Winds Over Vietnam, September 1970, ECOM-5346, AD 876935.
20. Rinehart, G. S., Humidity Generating Apparatus and Microscope Chamber for Use with Flowing Gas Atmospheres, October 1970, ECOM-5332, AD 716994.
21. Miers, B. T., R. O. Olsen, and E. P. Avara, Short Time Period Atmospheric Density Variations and a Determination of Density Errors from Selected Rocket-sonde Sensors, October 1970, ECOM-5335.
22. Rinehart, G. S., Sulfates and Other Water Solubles Larger than 0.15μ Radius in a Continental Nonurban Atmosphere, October 1970, ECOM-5336, AD 716999.
23. Lindberg, J. D., The Uncertainty Principle: A Limitation on Meteor Trail Radar Wind Measurements, October 1970, ECOM-5337, AD 716996.
24. Randhawa, J. S., Technical Data Package for Rocket-Borne Ozone-Temperature Sensor, October 1970, ECOM-5338, AD 716997.

25. Devine, J. C., The Fort Huachuca Climate Calendar, October 1970, ECOM-6054.
26. Allen, J. T., Meteorological Support to US Army RDT&E Activities, Fiscal Year 1970 Annual Report, November 1970, ECOM-6055.
27. Shinn, J. H., An Introduction to the Hyperbolic Diffusion Equation, November 1970, ECOM-5341, AD 718616.
28. Avara, E. P., and M. Kays, Some Aspects of the Harmonic Analysis of Irregularly Spaced Data, November 1970, ECOM-5344, AD 720193.
29. Fabrici, J., Inv. of Isotopic Emitter for Nuclear Barometer, November 1970, ECOM-3349, AD 876461.
30. Levine, J. R., Summer Mesoscale Wind Study in the Republic of Vietnam, December 1970, ECOM-3375, AD 721585.
31. Petriw, A., Directional Ion Anemometer, December 1970, ECOM-3379, AD 720573.
32. Randhawa, J. S., B. H. Williams, and M. D. Kays, Meteorological Influence of a Solar Eclipse on the Stratosphere, December 1970, ECOM-5345, AD 720199.
33. Nordquist, Walter S., Jr., and N. L. Johnson, One-Dimensional Quasi-Time-Dependent Numerical Model of Cumulus Cloud Activity, December 1970, ECOM-5350, AD 722216.
34. Avara, E. P., The Analysis of Variance of Time Series Data Part I: One-Way Layout, January 1971, ECOM-5352, AD 721594.
35. Avara, E. P., The Analysis of Variance of Time Series Data Part II: Two-Way Layout, January 1971, ECOM-5353.
36. Avara, E. P., and M. Kays, The Effect of Interpolation of Data Upon the Harmonic Coefficients, January 1971, ECOM-5354, AD 721593.
37. Randhawa, J. S., Stratosphere Diurnal Ozone Variation, January 1971, ECOM-5355, AD 721369.
38. Low, R. D. H., A Comprehensive Report on Nineteen Condensation Nuclei (Part II), January 1971, ECOM-5358.
39. Armendariz, M., L. J. Rider, G. Campbell, D. Favier and J. Serna, Turbulence Measurements from a T-Array of Sensors, February 1971, ECOM-5362, AD 726390.
40. Maynard, H., A Radix-2 Fourier Transform Program, February 1971, ECOM-5363, AD 726389.
41. Devine, J. C., Snowfalls at Fort Huachuca, Arizona, February 1971, ECOM-6056.
42. Devine, J. C., The Fort Huachuca, Arizona 15 Year Base Climate Calendar (1956-1970), February 1971, ECOM-6057.
43. Levine, J. R., Reduced Ceilings and Visibilities in Korea and Southeast Asia, March 1971, ECOM-3403, AD 722735.
44. Gerber, H., et al., Some Size Distribution Measurements of AgI Nuclei with an Aerosol Spectrometer, March 1971, ECOM-3414, AD 729331.
45. Engebos, B. F., and L. J. Rider, Vertical Wind Effects on the 2.75-inch Rocket, March 1971, ECOM-5365, AD 726321.
46. Rinehart, G. S., Evidence for Sulfate as a Major Condensation Nucleus Constituent in Nonurban Fog, March 1971, ECOM-5366.
47. Kennedy, B. W., E. P. Avara, and B. T. Miers, Data Reduction Program for Rocketsonde Temperatures, March 1971, ECOM-5367.
48. Hatch, W. H., A Study of Cloud Dynamics Utilizing Stereoscopic Photogrammetry, March 1971, ECOM-5368.
49. Williamson, L. E., Project Gun Probe Captive Impact Test Range, March 1971, ECOM-5369.
50. Henley, D. C., and G. B. Hoidale, Attenuation and Dispersion of Acoustic Energy by Atmospheric Dust, March 1971, ECOM-5370, AD 728103.
51. Cionco, R. M., Application of the Ideal Canopy Flow Concept to Natural and Artificial Roughness Elements, April 1971, ECOM-5372, AD 730638.
52. Randhawa, J. S., The Vertical Distribution of Ozone Near the Equator, April 1971, ECOM-5373.
53. Ethridge, G. A., A Method for Evaluating Model Parameters by Numerical Inversion, April 1971, ECOM-5374.

54. Collett, E., Stokes Parameters for Quantum Systems, April 1971, ECOM-3415, AD 729347.
55. Sninn, J. H., Steady-State Two-Dimensional Air Flow in Forests and the Disturbance of Surface Layer Flow by a Forest Wall, May 1971, ECOM-5383, AD 730681.
56. Müller, W. B., On Approximation of Mean and Variance-Covariance Matrices of Transformations of Joint Random Variables, May 1971, ECOM-5384, AD 730302.
57. Duncan, L. D., A Statistical Model for Estimation of Variability Variances from Noisy Data, May 1971, ECOM-5385.
58. Pries, T. H., and G. S. Campbell, Spectral Analyses of High-Frequency Atmospheric Temperature Fluctuations, May 1971, ECOM-5387.
59. Miller, W. B., A. J. Blanco, and L. E. Traylor, A Least-Squares Weighted-Layer Technique for Prediction of Upper Wind Effects on Unguided Rockets, June 1971, ECOM-5388, AD 729792.
60. Rubio, R., J. Smith and D. Maxwell, A Capacitance Electron Density Probe, June 1971, ECOM-5390.
61. Duncan, L. D., Redundant Measurements in Atmospheric Variability Experiments, June 1971, ECOM-5391.
62. Engebos, B. F., Comparisons of Coordinate Systems and Transformations for Trajectory Simulations, July 1971, ECOM-5397.
63. Hudlow, M. D., Weather Radar Investigations on an Artillery Test Conducted in the Panama Canal Zone, July 1971, ECOM-5411.
64. White, K. O., E. H. Holt, S. A. Schleusener, and R. F. Calfee, Erbium Laser Propagation in Simulated Atmospheres II. High Resolution Measurement Method, August 1971, ECOM-5396.
65. Waite, R., Field Comparison Between Sling Psychrometer and Meteorological Measuring Set AN/TMQ-22, August 1971, ECOM-5399.
66. Duncan, L. D., Time Series Editing By Generalized Differences, August 1971, ECOM-5400.
67. Reynolds, R. D., Ozone: A Synopsis of its Measurements and Use as an Atmospheric Tracer, August 1971, ECOM-5401.
68. Avara, E. P., and B. T. Miers, Noise Characteristics of Selected Wind and Temperature Data from 30-65 km, August 1971, ECOM-5402.
69. Avara, E. P., and B. T. Miers, Comparison of Linear Trends in Time Series Data Using Regression Analysis, August 1971, ECOM-5403.
70. Miller, W. B., Contributions of Mathematical Structure to the Error Behavior of Rawinsonde Measurements, August 1971, ECOM-5404.
71. Collett, E., Mueller Stokes Matrix Formulation of Fresnel's Equations, August 1971, ECOM-5480.
72. Armendariz, M., and L. J. Rider, Time and Space Correlation and Coherence in the Surface Boundary Layer, September 1971, ECOM-5407.
73. Avara, E. P., Some Effects of Randomization in Hypothesis Testing with Correlated Data, October 1971, ECOM-5408.
74. Randhawa, J. S., Ozone and Temperature Change in the Winter Stratosphere, November 1971, ECOM-5414.
75. Miller, W. B., On Approximation of Mean and Variance-Covariance Matrices of Transformations of Multivariate Random Variables, November 1971, ECOM-5413.
76. Horn, J. D., G. S. Campbell, A. L. Wallis (Capt., USAF), and R. G. McIntyre, Wind Tunnel Simulation and Prototype Studies of Barrier Flow Phenomena December 1971, ECOM-5416.
77. Dickson, David H., and James R. Oden, Fog Dissipation Techniques for Emergency Use, January 1972, ECOM-5420.
78. Ballard, H. N., N. J. Beyers, B. T. Miers, M. Izquierdo, and J. Whitacre, Atmospheric Tidal Measurements at 50 km from a Constant-Altitude Balloon, December 1971, ECOM-5417.
79. Miller, Walter B., On Calculation of Dynamic Error Parameters for the Rawinsonde and Related Systems, January 1972, ECOM-5422.

80. Richter, Thomas J., Rawin Radar Targets, February 1972, ECOM-5424.
81. Pena, Ricardo, L. J. Rider, and Manuel Armendariz, Turbulence Characteristics at Heights of 1.5, 4.0, and 16.0 Meters at White Sands Missile Range, New Mexico, January 1972, ECOM-5421.
82. Blanco, Abel J., and L. E. Traylor, Statistical Prediction of Impact Displacement due to the Wind Effect on an Unguided Artillery Rocket During Powered Flight, March 1972, ECOM-5427.
83. Williams, B. H., R. O. Olsen, and M. D. Kays, Stratospheric-Ionospheric Interaction During the Movement of a Planetary Wave in January 1967, March 1972, ECOM-5428.
84. Schleusener, Stuart A., and Kenneth O. White, Applications of Dual Parameter Analyzers in Solid-State Laser Tests, April 1972, ECOM-5432.
85. Pries, Thomas H., Jack Smith, and Marvin Hamiter, Some Observations of Meteorological Effects on Optical Wave Propagation, April 1972, ECOM-5434.
86. Dickson, D. H., Fogwash I An Experiment Using Helicopter Downwash, April 1972, ECOM-5431.
87. Mason, J. Z., and J. D. Lindberg, Laser Beam Behavior on a Long High Path, April 1972, ECOM-5430.
88. Smith, Jack, Thomas H. Pries, Kenneth J. Skipka, and Marvin Hamiter, Optical Filter Function for a Folded Laser Path, April 1972, ECOM-5433.
89. Lee, Robert P., Artillery Sound Ranging Computer Simulations, May 1972, ECOM-5441.
90. Lowenthal, Marvin J., The Accuracy of Ballistic Density Departure Tables 1934-1972, April 1972, ECOM-5436.
91. Cantor, Israel, Survey of Studies of Atmospheric Transmission from a 4- Light Source to a 2- Receiver, April 1972, ECOM-5435.
92. Barr, William C., Accuracy Requirements for the Measurement of Meteorological Parameters Which Affect Artillery Fire, April 1972, ECOM-5437.
93. Duchon, C. E., F. V. Brock, M. Armendariz, and J. D. Horn, UVW Anemometer Dynamic Performance Study, May 1972, ECOM-5440.
94. Gomez, R. B., Atmospheric Effects for Ground Target Signature Modeling I. Atmospheric Transmission at 1.06 Micrometers, June 1972, ECOM-5445.
95. Bonner, R. S., A Technical Manual on the Characteristics and Operation of a Cloud Condensation Nuclei Collection/Detection/Recording Instrument, June 1972, ECOM-5447.
96. Horn, J. D., R. D. Reynolds, and T. H. Vonder Haar, Survey of Techniques Used in Display of Sequential Images Received from Geostationary Satellites, June 1972, ECOM-5450.
97. Bonner, R. S., and H. M. White, Microphysical Observations of Fog in Redwood Valley near Arcata-Eureka, California, July 1972, ECOM-5455.
98. Waite, R. W., Reliability Test of Electronics Module of Meteorological Measuring Set AN.TMQ-22(XE-4), June 1972, ECOM-5448.
99. Doswell, C. A., III, An Iterative Method for Saturation Adjustment, June 1972, ECOM-5441.
100. Doswell, C. A., III, A Two-Dimensional Short-Range Fog Forecast Model, May 1972, ECOM-5443.
101. Seagraves, Mary Ann B., A General-Purpose Meteorological Rocket Data Reduction Program, August 1972, ECOM-5463.
102. Loveland, Loveland, R. B., J. L. Johnson, and B. D. Hinds, Differential Magnetic Measurements Near Cumulus Clouds, August 1972, ECOM-5463.
103. Cantor, Israel, and Michael Hudlow, Rainfall Effects on Satellite Communications in the K, X, and C Bands, July 1972, ECOM-5459.
104. Randhawa, J. S., Variations in Stratospheric Circulation and Ozone During Selected Periods, August 1972, ECOM-5460.
105. Rider, L. J., Armendariz, Manuel, Mean Horizontal Wind Speed and Direction Variability at Heights of 1.5 and 4.0 Meters Above Ground Level at WSMR, New Mexico, October 1972, ECOM-5466.

106. Nordquist, Walter S., Jr., and Dickson, David H., Helicopter Downwash Applied to Fog Clearing: A Status Summary, October 1972, ECOM-5465.
107. Engebos, Bernard F., Effects of Vertical Wind on Tactical Rockets and Artillery Shells, November 1972, ECOM-5467.
108. Armendariz, M., and James R. Scoggins, Characteristics of the Turbulent Diffusion Parameters as Related to Stability, November 1972, ECOM-5468.